NCERT QUESTIONS WITH SOLUTIONS

FIGURE IT OUT-01

1. Which of the following numbers are not perfect squares?

(i) 2032 (ii) 2048
(iii) 1027 (iv) 1089

Sol. (i) 2032 is not a perfect square, as a number ending with 2 cannot be a perfect square.

(ii) 2048 is not a perfect square, as a number ending with 8 cannot be a perfect square.

(iii) 1027 is not a perfect square, as a number ending with 7 cannot be a perfect square.

(iv) 1089 ends in 9 at the unit's place. Hence, it is a perfect square.

2. Which one among 64^2, 108^2, 292^2, 36^2 has the last digit 4?

Sol. (i) Unit's digit of 64 is 4

$\therefore$ $4^2 = 4 \times 4 = 16$ (last digit = 6)

(ii) Unit's digit of 108 is 8

$\therefore$ $8^2 = 8 \times 8 = 64$ (last digit = 4)

(iii) Unit's digit of 292 is 2

$\therefore$ $2^2 = 2 \times 2 = 4$

(iv) Unit's digit of 36 = 6

$\therefore$ $6^2 = 6 \times 6 = 36$ (last digit = 6)

Hence, the numbers whose squares end in 4 are 108^2 and 292^2.

3. Given $125^2 = 15625$, what is the value of 126^2?

(i) $15625 + 126$ (ii) $15625 + 26^2$
(iii) $15625 + 253$ (iv) $15625 + 251$
(v) $15625 + 51^2$

Sol. Here, $126^2 = (125 + 1)^2$

$= (125)^2 + 2 \times 125 \times 1 + (1)^2$

[Using identity $(a + b)^2 = a^2 + 2ab + b^2$]

$= 15625 + 250 + 1$

$= 15625 + 251$

So, the value of 126^2 is (iv) option, i.e., 15625 + 251.

4. Find the length of the side of a square whose area is 441 m^2.

Sol. Area of square = side × side = 441

$\Rightarrow$ $\text{side}^2 = 441$

$\Rightarrow$ $\text{side} = \sqrt{441}$

3	441
3	147
7	49
7	7
	1

$441 = \underline{3 \times 3} \times \underline{7 \times 7}$

$\sqrt{441} = 3 \times 7 = 21$

$\therefore$ Side of square = 21 m.

5. Find the smallest square number that is divisible by each of the following numbers: 4, 9, and 10.

Sol. To find the required smallest square number, we will find the least number divisible by each of 4, 9, and 10, i.e., LCM of 4, 9, and 10.

2	4,	9,	10
2	2,	9,	5
3	1,	9,	5
3	1,	3,	5
5	1,	1,	5
	1,	1,	1

LCM = $2 \times 2 \times 3 \times 3 \times 5 = 180$

Prime factorisation of 180 = $2\times2\times3\times3\times5$

5 is not in pairs, so 180 is not a square number.

In order to get a perfect square, we will multiply 180 by 5.

So, the required smallest square number is 900.

6. Find the smallest number by which 9408 must be multiplied so that the product is a perfect square. Find the square root of the product.

Sol.

2	9408
2	4704
2	2352
2	1176
3	588
3	294
3	147
7	49
7	7
	1

$9408 = 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 7 \times 7$

All prime factors of 9408 are arranged in pairs except 3.

So, we multiply 9408 by 3 to make it a perfect square.

Perfect square = $9408 \times 3 = 28224$

Now,

$\sqrt{28224} = \sqrt{2\times2\times2\times2\times3\times3\times3\times3\times7\times7}$

$= 2 \times 2 \times 3 \times 3 \times 7$

$= 252$

7. How many numbers lie between the squares of the following numbers?

(i) 16 and 17 (ii) 99 and 100

Sol. (i) Numbers lying between 16^2 and 17^2

$= 2 \times 16 = 32$

(ii) Numbers lying between 99^2 and 100^2

$= 2 \times 99 = 198$

8. In the following pattern, fill in the missing numbers:

$1^2 + 2^2 + 2^2 = 3^2$

$2^2 + 3^2 + 6^2 = 7^2$

$3^2 + 4^2 + 12^2 = 13^2$

$4^2 + 5^2 + 20^2 = (\_\_)^2$

$9^2 + 10^2 + (\_\_)^2 = (\_\_)^2$

Sol. $1^2 + 2^2 + 2^2 = 3^2$

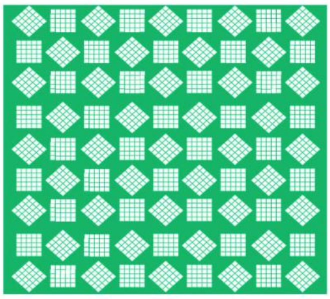
$2^2 + 3^2 + 6^2 = 7^2$

$3^2 + 4^2 + 12^2 = 13^2$

$4^2 + 5^2 + 20^2 = 21^2$

$9^2 + 10^2 + 90^2 = 91^2$

9. How many tiny squares are there in the following picture? Write the prime factorisation of the number of tiny squares.



Sol. Big squares in a row = 9

Big squares in a column = 9

Tiny squares in a big square = 25

$\therefore$ Total tiny squares = $9 \times 9 \times 25 = 2025$

Now prime factorisation of 2025

$= 3 \times 3 \times 3 \times 3 \times 5 \times 5$

FIGURE IT OUT-02

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1. Find the cube roots of 27000 and 10648.

Sol. Here,

2	27000
2	13500
2	6750
3	3375
3	1125
3	375
5	125
5	25
5	5
	1

$27000 = \underline{2 \times 2 \times 2} \times \underline{3 \times 3 \times 3} \times \underline{5 \times 5 \times 5}$

$\sqrt[3]{27000} = 2 \times 3 \times 5 = 30$

2	10648
2	5324
2	2662
11	1331
11	121
11	11
	1

$10648 = 2 \times 2 \times 2 \times 11 \times 11 \times 11$

$\sqrt[3]{10648} = 2 \times 11 = 22$

2. What number will you multiply by 1323 to make it a cube number?

Sol. Here,

3	1323
3	441
3	147
7	49
7	7
	1

$1323 = 3 \times 3 \times 3 \times 7 \times 7$

To complete the triplet, one more 7 is required.

So, 1323 will be multiplied by 7 to make it a cube number.

So, the cube number = $1323 \times 7 = 9261$

Hence, required number = 7

3. State true or false. Explain your reasoning.

(i) The cube of any odd number is even.

(ii) There is no perfect cube that ends with 8.

(iii) The cube of a 2-digit number may be a 3-digit number.

(iv) The cube of a 2-digit number may have seven or more digits.

(v) Cube numbers have an odd number of factors.

Sol. (i) The cube of any odd number is even. (False)

Reason: The cube of an odd number is always odd, as

$3^3 = 27$

$5^3 = 125$

$7^3 = 343$

(ii) There is no perfect cube that ends with 8. (False)

Reason: The cubes of all the numbers ending with 2 at the unit place end with 8.

$2^3 = 8$

$12^3 = 1728$

$22^3 = 10648$

(iii) The cube of a 2-digit number may be a 3-digit number. (False)

Reason: Cube of a 2-digit number may have a minimum of 4 digits to a maximum of 6 digits.

10 is the smallest 2-digit number, and $10^3 = 1000$, which has 4 digits.

(iv) The cube of a 2-digit number may have seven or more digits. (False)

Reason: Cube of a 2-digit number may have at most 6 digits.

99 is the largest 2-digit number, and $99^3 = 970299$, which is a 6-digit number.

(v) Cube numbers have an odd number of factors. (False)

Reason: Cube numbers may have an odd as well as an even number of factors.

As $27 = 3 \times 3 \times 3$ (odd no. of factors)

$64 = 2 \times 2 \times 2 \times 2 \times 2 \times 2$ (even no. of factors)

4. You are told that 1331 is a perfect cube. Can you guess without factorisation what its cube root is? Similarly, guess the cube roots of 4913, 12167, and 32768.

Sol. To find the cube root of 1331,

1331

We divide the given number 1331 into two groups, starting from the right side, taking three digits in group 1.

331 → group 1

1 → group 2

331 → unit digit is 1

Hence, the cube roots of one's digit is 1 .....(1)

Group 2, i.e., 1 only, which is 1^3.

So, the cube roots of one's digit is 1. ...(2)

$\because \sqrt[3]{1331} = 11$

4913

Group 1 – 913

Group 2 – 4

Unit digit of 913 is 3.

We know that 3 comes at the unit's place when its cube root ends in 7, as $7 \times 7 \times 7 = 343$

So the unit digit of the cube root of 4913 = 7 .....(1)

Group 2 – 4

4 lies between 1 (i.e., 1^3) and 2^3 (i.e., 8)

$1^3 < 4 < 2^3$

Taking the lower limit, the tens digit of the cube root of 4913 is 1. .....(2)

$\sqrt[3]{4913} = 17$ (from (1) & (2))

12167

Group 1 – 167

Unit digit = 7

So, unit digit of cube root of 12167 = 3 as $3 \times 3 \times 3 = 27$

Group 2 – 12

$8 < 12 < 27$

$2^3 < 12 < 3^3$

Taking the lower limit, the ten's digit of cube root = 2

So, $\sqrt[3]{12167} = 23$

32768

Group 1 – 768

Unit digit = 8

So unit digit of cube root of 32768 = 2 .....(1)

as $2 \times 2 \times 2 = 8$

$\Rightarrow \sqrt[3]{8} = 2$

From Group 2 – 32

$27 < 32 < 64$

$3^3 < 32 < 4^3$

Taking lower limit, ten's digit of the cube root of 32768 is 3. .....(2)

$\therefore \sqrt[3]{32768} = 32$ (from (1) & (2))

5. Which of the following is the greatest? Explain your reasoning.

(i) $67^3 - 66^3$

(ii) $43^3 - 42^3$

(iii) $67^2 - 66^2$

(iv) $43^2 - 42^2$

Sol. (i) $67^3 - 66^3 = 1 + 67 \times 66 \times 3$

(ii) $43^3 - 42^3 = 1 + 43 \times 42 \times 3$

(iii) $67^2 - 66^2 = 67 + 66 = 133$

(iv) $43^2 - 42^2 = 43 + 42 = 85$

From above we can see that $67^3 - 66^3$ is the greatest as

$(n + 1)^3 - n^3 = 1 + (n + 1) \times 3n$

$(n + 1)^2 - n^2 = n + n + 1 = 2n + 1$