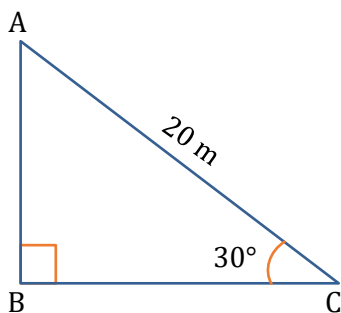


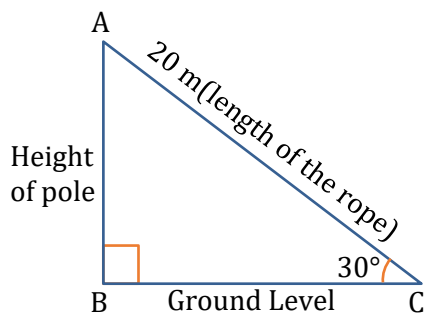
NCERT QUESTIONS WITH SOLUTIONS

EXERCISE : 9.1

1. A circus artist is climbing a 20 m long rope, which is tightly stretched and tied from the top of a vertical pole to the ground. Find the height of the pole if the angle made by the rope with the ground level is 30° (see fig.).



Sol. $AC = 20$ m is the length of the rope.
 Let $AB = h$ metres be the height of the pole
 $\angle ACB = 30^\circ$ (Given)



Now,

$$\frac{AB}{AC} = \sin 30^\circ = \frac{1}{2}$$

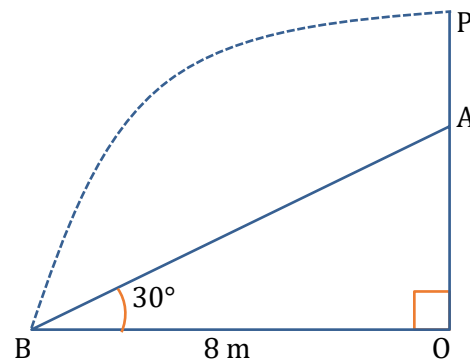
$$\Rightarrow \frac{h}{20} = \frac{1}{2}$$

$$\Rightarrow h = 10 \text{ m}$$

\therefore the height of the pole is 10 m.

2. A tree breaks due to storm and the broken part bends so that the top of the tree touches the ground making an angle of 30° with the ground. The distance between the foot of the tree to the point where the top touches the ground is 8 m. Find the height of the tree.

Sol.



Let tree is broken at A and its top is touching the ground at B.

Now, in right $\triangle AOB$, we have

$$\frac{AO}{OB} = \tan 30^\circ$$

$$\Rightarrow \frac{AO}{8} = \frac{1}{\sqrt{3}}$$

$$\Rightarrow AO = \frac{8}{\sqrt{3}} \text{ m}$$

Also, $\frac{AB}{OB} = \sec 30^\circ$

$$\Rightarrow \frac{AB}{8} = \frac{2}{\sqrt{3}}$$

$$\Rightarrow AB = \frac{2 \times 8}{\sqrt{3}} = \frac{16}{\sqrt{3}} \text{ m}$$

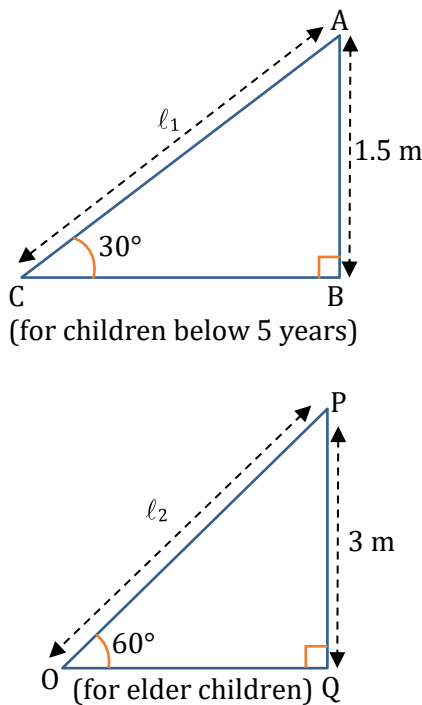
Now, height of the tree $OP = OA + AP$
 $= OA + AB$

$$= \frac{8}{\sqrt{3}} + \frac{16}{\sqrt{3}} = \frac{24}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} \text{ m} = 8\sqrt{3} \text{ m}$$

\therefore the height of the tree is $8\sqrt{3}$ m

3. A contractor plans to install two slides for the children to play in a park. For the children below the age of 5 years, she prefers to have a slide whose top is at a height of 1.5 m and is inclined at an angle of 30° to the ground, whereas for elder children, she wants to have a steep slide at a height of 3 m and is inclined at an angle of 60° to the ground. What should be the length of the slide in each case?

Sol. In figure, l_1 is the length of the slide made for children below the age of 5 years and l_2 is the length of the slide made for elder children.



In figure, $AB = 1.5$ m, $AC = l_1$ m and $\angle ACB = 30^\circ$, $PQ = 3$ m, $OP = l_2$ m and $\angle POQ = 60^\circ$

$$\frac{AB}{AC} = \sin 30^\circ \text{ and } \frac{PQ}{OP} = \sin 60^\circ$$

$$\Rightarrow \frac{1.5}{l_1} = \frac{1}{2} \text{ and } \frac{3}{l_2} = \frac{\sqrt{3}}{2}$$

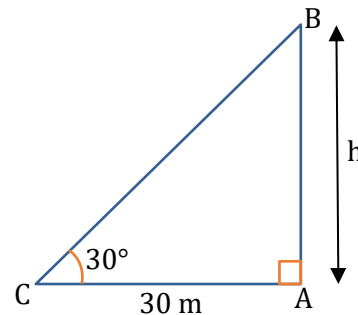
$$\Rightarrow l_1 = 2 \times 1.5 \text{ m and } l_2 = \frac{3 \times 2}{\sqrt{3}} \text{ m}$$

$$\Rightarrow l_1 = 3 \text{ m and } l_2 = 2\sqrt{3} \text{ m}$$

\therefore the length of the slides are 3m and $2\sqrt{3}$ m respectively.

4. The angle of elevation of the top of a tower from a point on the ground which is 30 m away from the foot of the tower, is 30° . Find the height of the tower.

Sol. In right $\triangle ABC$, $AB = h$ height of the tower and point C is 30m away from the foot of the tower,



$$\therefore AC = 30 \text{ m}$$

$$\text{Now, } \frac{AB}{AC} = \tan 30^\circ$$

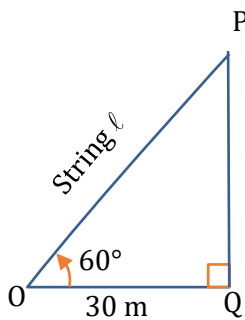
$$\Rightarrow \frac{h}{30} = \frac{1}{\sqrt{3}}$$

$$\Rightarrow h = \frac{30}{\sqrt{3}} = \frac{30}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} = 10\sqrt{3}$$

Thus, the required height of the tower is $10\sqrt{3}$ m.

5. A kite is flying at a height of 60 m above the ground. The string attached to the kite is temporarily tied to a point on the ground. The inclination of the string with the ground is 60° . Find the length of the string, assuming that there is no slack in the string.

Sol. P is the position of the kite. Its height from the point Q (on the ground) = $PQ = 60$ m



Let $OP = l$ be the length of the string.

$$\angle POQ = 60^\circ \text{ (Given)}$$

$$\text{Now, } \frac{PQ}{OP} = \sin 60^\circ$$

$$\Rightarrow \frac{60}{l} = \sin 60^\circ = \frac{\sqrt{3}}{2}$$

$$\Rightarrow \frac{60}{l} = \frac{\sqrt{3}}{2}$$

$$\Rightarrow l = 40\sqrt{3} \text{ m}$$

\therefore the length of the string is $40\sqrt{3}$ m.

6. A 1.5 m tall boy is standing at some distance from a 30 m tall building. The angle of elevation from his eyes to the top of the building increases from 30° to 60° as he walks towards the building. Find the distance he walked towards the building.

Sol. $PQ = 30$ m is the height of the building.

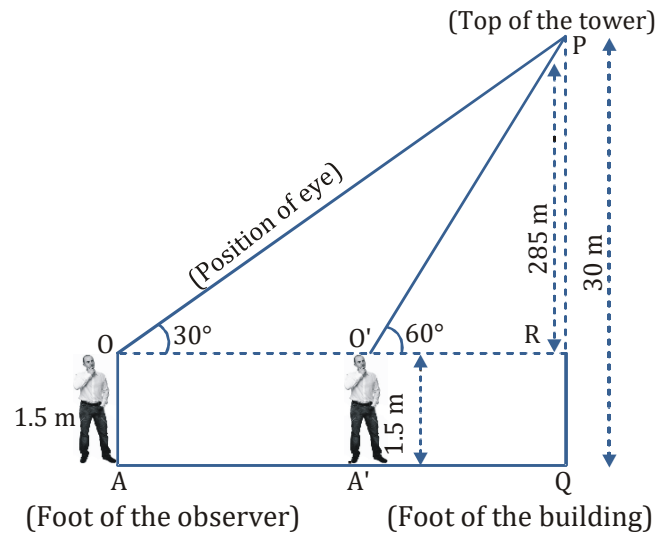
$OA = 1.5$ m is the height of the boy. Its first position is at OA . OR is horizontal line through the position of the eye at O .

$$\angle POR = 30^\circ \text{ (Given)}$$

The second position of the boy is at $O'A'$ and $\angle PO'R = 60^\circ$.

$$\text{Here, } RQ = OA = O'A' = 1.5 \text{ m}$$

$$\text{and } PR = 30 \text{ m} - 1.5 \text{ m} = 28.5 \text{ m}$$



In $\triangle POR$,

$$\frac{PR}{OR} = \tan 30^\circ$$

$$\Rightarrow \frac{28.5}{OR} = \frac{1}{\sqrt{3}}$$

$$\Rightarrow OR = 28.5\sqrt{3} \text{ m}$$

$$\Rightarrow O'R = \frac{28.5}{\sqrt{3}} \text{ m}$$

In $\triangle PO'R$,

$$\frac{PR}{O'R} = \tan 60^\circ$$

$$\Rightarrow \frac{28.5}{O'R} = \sqrt{3}$$

$$\dots \text{ (i)}$$

$$\dots \text{ (ii)}$$

The distance walked by the boy towards the building = $OO' = OR - O'R$

[From (i) and (ii)]

$$= 28.5 \times \sqrt{3} \text{ m} - \frac{28.5}{\sqrt{3}} \text{ m}$$

$$= 28.5 \times \left\{ \sqrt{3} - \frac{1}{\sqrt{3}} \right\} \text{ m}$$

$$= 28.5 \times \frac{(3-1)}{\sqrt{3}} \text{ m} = 28.5 \times \frac{2}{\sqrt{3}} \text{ m}$$

$$= \frac{57}{\sqrt{3}} \text{ m} = 19\sqrt{3} \text{ m}$$

∴ the boy walks $19\sqrt{3}$ m towards the building.

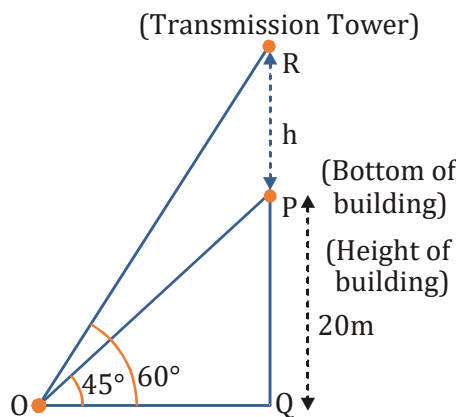
7. From a point on the ground, the angles of elevation of the bottom and the top of a transmission tower fixed at the top of a 20m high building are 45° and 60° respectively. Find the height of the tower.

Sol. $PQ = 20$ m is the height of the building.

Let $PR = h$ metres be the height of the transmission tower. P is the bottom and R is the top of the transmission tower.

$\angle POQ = 45^\circ$ and $\angle ROQ = 60^\circ$

In $\triangle OPQ$,



$$\frac{PQ}{OQ} = \tan 45^\circ$$

$$\Rightarrow \frac{20}{OQ} = 1$$

$$\Rightarrow OQ = 20 \text{ m}$$

In $\triangle ORQ$,

$$\frac{RQ}{OQ} = \tan 60^\circ$$

$$\Rightarrow \frac{20+h}{20} = \sqrt{3}$$

(∵ $RQ = PQ + PR = 20 + h$ metres and $OQ = 20$ metres)

$$\Rightarrow 1 + \frac{h}{20} = \sqrt{3}$$

$$\Rightarrow \frac{h}{20} = (\sqrt{3} - 1)$$

$$\Rightarrow h = 20(\sqrt{3} - 1) \text{ m}$$

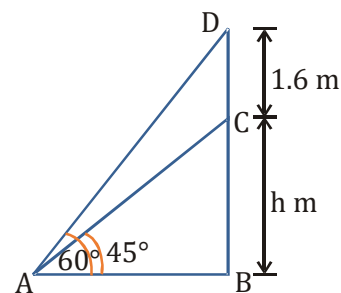
∴ the height of the tower is $20(\sqrt{3} - 1)$ m.

8. A statue, 1.6 m tall, stands on the top of pedestal. From a point on the ground, the angle of elevation of the top of the statue is 60° and from the same point the angle of elevation of the top of the pedestal is 45° . Find the height of the pedestal.

Sol. In the figure, DC represents the statue and BC represents the pedestal.

Let the height of pedestal is 'h'

Now, in right $\triangle ABC$, we have



$$\frac{AB}{BC} = \cot 45^\circ = 1$$

$$\Rightarrow \frac{AB}{h} = 1$$

$$\Rightarrow AB = h \text{ metres} \quad \dots (i)$$

Now in right $\triangle ABD$, we have

$$\frac{BD}{AB} = \tan 60^\circ = \sqrt{3}$$

$$\Rightarrow BD = \sqrt{3} \times AB = \sqrt{3} \times h \text{ [from (i)]}$$

$$\Rightarrow h + 1.6 = \sqrt{3} h$$

$$\Rightarrow h(\sqrt{3} - 1) = 1.6$$

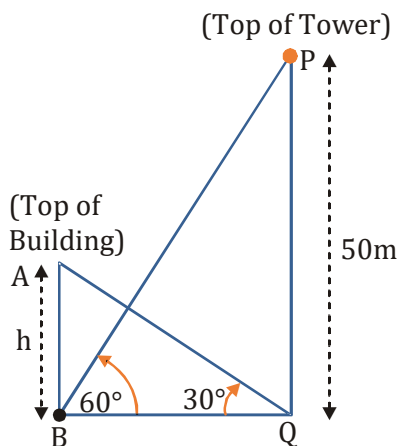
$$\Rightarrow h = \frac{1.6}{\sqrt{3} - 1} = \frac{1.6}{\sqrt{3} - 1} \times \frac{\sqrt{3} + 1}{\sqrt{3} + 1}$$

$$\begin{aligned} \Rightarrow h &= \frac{1.6}{3 - 1} \times (\sqrt{3} + 1) = \frac{1.6}{2} \times (\sqrt{3} + 1) \\ &= 0.8(\sqrt{3} + 1)\text{m} \end{aligned}$$

Thus, the height of the pedestal is $0.8(\sqrt{3} + 1)\text{m}$.

9. The angle of elevation of the top of a building from the foot of the tower is 30° and the angle of elevation of the top of the tower from the foot of the building is 60° . If the tower is 50 m high, find the height of the building.

Sol. $PQ = 50$ metres is the height of the tower. Let $AB = h$ metres be the height of the building. Angle of elevation of the top of the building from the foot of the tower = 30° , i.e., $\angle AQB = 30^\circ$.



Angle of elevation of the top of the tower from the foot of the building = 60° , i.e., $\angle PBQ = 60^\circ$.

In $\triangle AQB$, $\frac{AB}{BQ} = \tan 30^\circ$

$$\frac{h}{BQ} = \frac{1}{\sqrt{3}}$$

$$\Rightarrow BQ = h\sqrt{3} \quad \dots \text{(i)}$$

In $\triangle PBQ$

$$\frac{50}{BQ} = \tan 60^\circ = \sqrt{3}$$

$$\Rightarrow BQ = \frac{50}{\sqrt{3}} \quad \dots \text{(ii)}$$

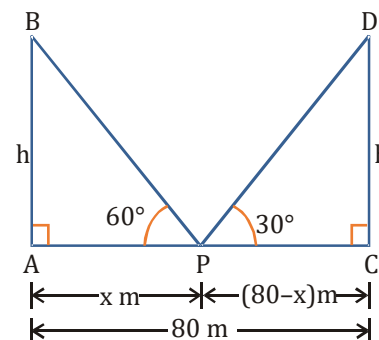
From (i) and (ii), we have $h\sqrt{3} = \frac{50}{\sqrt{3}}$

$$\Rightarrow h = \frac{50}{3}\text{m} \quad \text{i.e., } h = 16\frac{2}{3}\text{m}$$

\therefore the height of building is $16\frac{2}{3}\text{m}$.

10. Two poles of equal heights are standing opposite to each other on either side of the road, which is 80 m wide. From a point between them on the road, the angles of elevation of the top of the poles are 60° and 30° respectively. Find the height of the poles and the distance of the point from the poles.

Sol. Let AB and CD be two poles and P is the point in between them.



$$\begin{aligned}
 &AB = h \text{ metres} \\
 \Rightarrow &CD = h \text{ metres} \\
 &AP = x \text{ m} \\
 \Rightarrow &CP = (80 - x) \text{ m} \\
 \text{Now, in right } \triangle APB, &\text{ we have} \\
 \frac{AB}{AP} = \tan 60^\circ &\Rightarrow \frac{h}{x} = \sqrt{3} \\
 \Rightarrow h = \sqrt{3}x &\dots \text{ (i)}
 \end{aligned}$$

$$\begin{aligned}
 \text{Again, in right } \triangle CPD, &\text{ we have} \\
 \frac{CD}{CP} = \tan 30^\circ & \\
 \Rightarrow \frac{h}{(80-x)} = \frac{1}{\sqrt{3}} & \\
 \Rightarrow h = \frac{80-x}{\sqrt{3}} &\dots \text{ (ii)}
 \end{aligned}$$

$$\begin{aligned}
 \text{From (i) and (ii), we get} & \\
 \sqrt{3}x = \frac{80-x}{\sqrt{3}} & \\
 \Rightarrow \sqrt{3} \times \sqrt{3} \times x = 80 - x &\Rightarrow 3x = 80 - x \\
 \Rightarrow 3x + x = 80 \Rightarrow 4x = 80 &\Rightarrow x = \frac{80}{4} = 20 \\
 \therefore CP = 80 - x = 80 - 20 = 60 \text{ m} &
 \end{aligned}$$

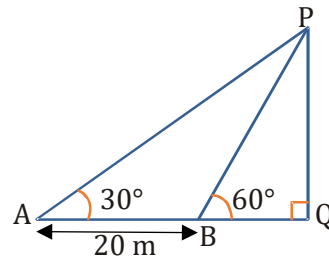
$$\begin{aligned}
 \text{Now, from (i), we have} & \\
 h = \sqrt{3} \times 20 = 1.732 \times 20 = 34.64 &
 \end{aligned}$$

Thus, the required point is 20 m away from the first pole and 60 m away from the second pole.

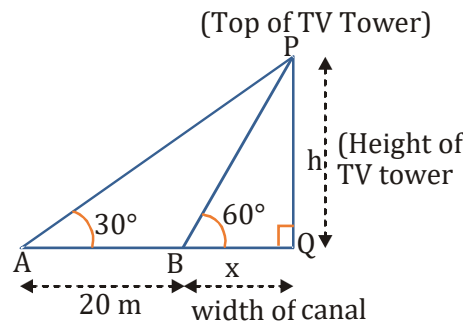
Height of each pole = 34.64 m.

11. A TV tower stands vertically on a bank of a canal. From a point on the other bank directly opposite the tower, the angle of elevation of the top of the tower is 60° . From another point 20 m away from this point on the line joining this point to the foot of the tower, the angle of elevation of

the top of the tower is 30° (see fig.). Find the height of the tower and the width of the canal.



Sol. Let $PQ = h$ metres be the height of the tower and $BQ = x$ metres be the width of the canal $\angle PBQ = 60^\circ$



Now, the angle of elevation of the top of the tower from the point A is 30° . i.e., $\angle PAQ = 30^\circ$ where $AB = 20$ metres.

$$\begin{aligned}
 \text{In } \triangle PBQ, & \\
 \frac{h}{x} = \tan 60^\circ &\Rightarrow \frac{h}{x} = \sqrt{3} \\
 \Rightarrow h = \sqrt{3}x &\dots \text{ (i)}
 \end{aligned}$$

$$\begin{aligned}
 \text{In } \triangle PAQ, & \\
 \frac{h}{20+x} = \tan 30^\circ = \frac{1}{\sqrt{3}} & \\
 \Rightarrow h = \frac{20+x}{\sqrt{3}} &\dots \text{ (ii)}
 \end{aligned}$$

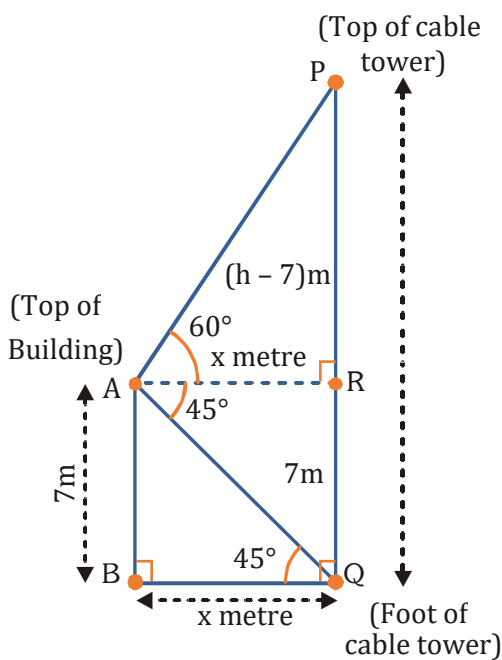
$$\begin{aligned}
 \text{From (i) and (ii), we have } \sqrt{3}x &= \frac{20+x}{\sqrt{3}} \\
 \Rightarrow 3x = 20 + x & \\
 \Rightarrow 2x = 20 \Rightarrow x = 10 & \\
 \text{From (i), } h = 10\sqrt{3} \text{ m} & \\
 \therefore \text{ the height of tower is } 10\sqrt{3} \text{ m and} & \\
 \text{width of canal is } 10 \text{ m.} &
 \end{aligned}$$

12. From the top of a 7 m high building, the angle of elevation of the top of a cable tower is 60° and the angle of depression of its foot is 45° . Determine the height of the tower.

Sol. Let $PQ = h$ metres be the height of the cable tower.

$AB = 7$ metres is the height of the building
 $\angle PAR = 60^\circ$ is the angle of elevation of the top of the cable tower from the top of the building.

$\angle RAQ = 45^\circ$ is the angle of depression of the foot of the cable tower from the top of the building. Then $\angle AQB = 45^\circ$.



Now, $BQ = AR = x$ metres (say)

$$\text{In } \triangle AQB, \frac{AB}{BQ} = \tan 45^\circ \Rightarrow \frac{7}{x} = 1 \Rightarrow x = 7 \text{ m}$$

Now, in $\triangle PAR$,

$$\frac{PR}{AR} = \tan 60^\circ$$

$$\Rightarrow \frac{PQ - QR}{x} = \sqrt{3}$$

$$\Rightarrow \frac{h-7}{x} = \sqrt{3}$$

$$\Rightarrow \frac{h-7}{x} = \sqrt{3}$$

$$\Rightarrow h = 7(\sqrt{3} + 1)$$

Hence, the height of the cable tower is $7(\sqrt{3} + 1)$ metre.

13. As observed from the top of a 75 m high lighthouse from the sea-level, the angles of depression of two ships are 30° and 45° . If one ship is exactly behind the other on the same side of the lighthouse, find the distance between the two ships.

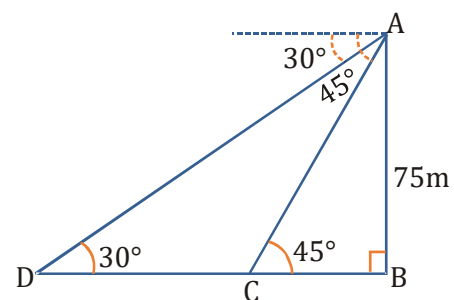
Sol. In the figure, let AB represent the lighthouse.

$$\therefore AB = 75 \text{ m}$$

Let the two ships be C and D such that angle of depression from A are 45° and 30° respectively.

Now, in right $\triangle ABC$, we have

$$\frac{AB}{BC} = \tan 45^\circ$$



$$\Rightarrow \frac{75}{BC} = 1$$

$$\Rightarrow BC = 75 \text{ m}$$

Again, in right $\triangle ABD$, we have

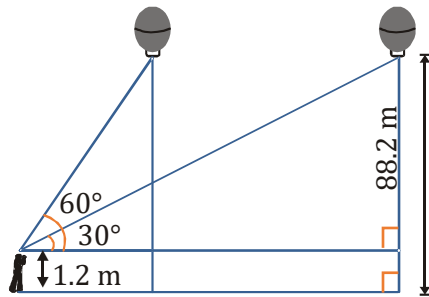
$$\frac{AB}{BD} = \tan 30^\circ$$

$$\Rightarrow \frac{75}{BD} = \frac{1}{\sqrt{3}}$$

$$\Rightarrow BD = 75\sqrt{3} \text{ m}$$

Since the distance between the two ships = $CD = BD - BC = 75\sqrt{3} - 75 = 75(\sqrt{3} - 1) = 75(1.732 - 1) = 75 \times 0.732 = 54.9 \text{ m}$
Thus, the required distance between the ships is 54.9 m.

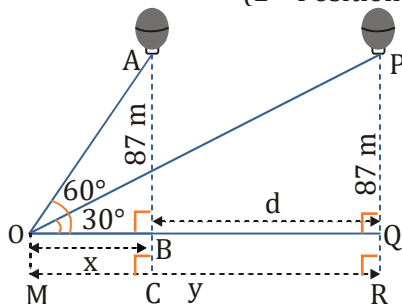
14. A 1.2 m tall girl spots a balloon moving with the wind in a horizontal line at a height of 88.2 m from the ground. The angle of elevation of the balloon from the eyes of the girl at any instant is 60° . After some time, the angle of elevation reduces to 30° (see figure). Find the distance travelled by the balloon during the interval.



Sol. From figure, we have $\angle AOB = 60^\circ$ is the angle of elevation for the first position of the balloon. Let $OB = x \text{ m}$.

(1st Position of balloon)

(2nd Position of balloon)



We are given that

$$AC = 88.2 \text{ m}, AB = 88.2 - 1.2 = 87 \text{ m}$$

For the second position of the balloon, we have

$$\angle POQ = 30^\circ. \text{ Let } OQ = y$$

We have to find distance $d = BQ = (y - x)$

$$\frac{AB}{OB} = \tan 60^\circ \text{ and } \frac{PQ}{OQ} = \tan 30^\circ$$

$$\Rightarrow \frac{87}{x} = \sqrt{3} \text{ and } \frac{87}{y} = \frac{1}{\sqrt{3}}$$

$$\Rightarrow x = \frac{87}{\sqrt{3}} \text{ m and } y = 87\sqrt{3} \text{ m}$$

$$\text{Now, } d = y - x = \left\{ 87\sqrt{3} - \frac{87}{\sqrt{3}} \right\} \text{ m}$$

$$= 87 \times \left\{ \sqrt{3} - \frac{1}{\sqrt{3}} \right\} \text{ m}$$

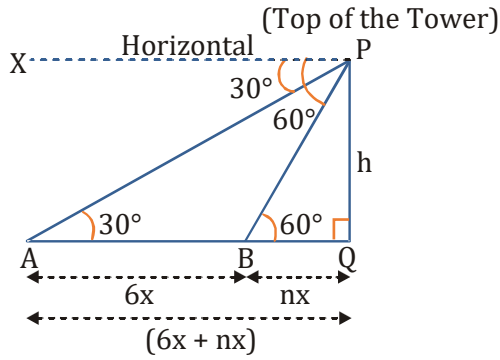
$$= 87 \times \frac{2}{\sqrt{3}} \text{ m} = 87 \times \frac{2}{3} \times \sqrt{3} \text{ m}$$

$$= \frac{174}{3} \sqrt{3} \text{ m} = 58\sqrt{3} \text{ m}$$

\therefore A distance travelled by the balloon during interval is $58\sqrt{3} \text{ m}$.

15. A straight highway leads to the foot of a tower. A man standing at the top of the tower observes a car at an angle of depression of 30° , which is approaching the foot of the tower with a uniform speed. Six seconds later, the angle of depression of the car is found to be 60° . Find the time taken by the car to reach the foot of the tower from this point.

Sol. Let $PQ = h$ metres be the height of the tower. P is the top of the tower. PX is horizontal line through P. The first and second positions of the car are at A and B respectively.



$$\angle APX = 30^\circ$$

Angles of depression of the car when observed at A and B are $\angle APX = 30^\circ$ and $\angle BPX = 60^\circ$ respectively.

Then, $\angle PAQ = 30^\circ$ and $\angle PBQ = 60^\circ$

Let the speed of the car be x m/sec

Then, distance $AB = 6x$ m

Let the time taken from B to Q be n seconds.

Then distance $BQ = nx$ m

In right $\triangle PAQ$ $\frac{h}{6x + nx} = \tan 30^\circ = \frac{1}{\sqrt{3}}$ $\Rightarrow h = \frac{(n+6)x}{\sqrt{3}} \dots(i)$	In right $\triangle PBQ$ $\frac{h}{nx} = \tan 60^\circ = \sqrt{3}$ $\Rightarrow h = nx\sqrt{3} \dots(ii)$
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From (i) and (ii), we have

$$\frac{(n+6)x}{\sqrt{3}} = nx\sqrt{3}$$

$$\Rightarrow n + 6 = n\sqrt{3} \times \sqrt{3}$$

$$\Rightarrow 3n = n + 6$$

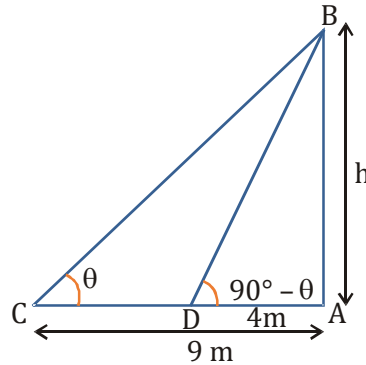
$$\Rightarrow 2n = 6$$

$$\Rightarrow n = 3$$

Hence, the time taken to travel from B to Q = 3 seconds.

16.** The angles of elevation of the top of a tower from two points at a distance of 4 m and 9 m from the base of the tower and in the same straight line with it are complementary. Prove that the height of the tower is 6 m.

Sol. Let the tower be represented by AB in the figure.



Let $AB = h$ metres.

$$\therefore \text{ In right } \triangle ABC, \text{ we have } \frac{AB}{AC} = \tan \theta$$

$$\Rightarrow \frac{h}{9} = \tan \theta \dots(i)$$

In right $\triangle ABD$, we have

$$\frac{AB}{AD} = \tan(90^\circ - \theta) = \cot \theta$$

$$\Rightarrow \frac{h}{4} = \cot \theta \dots(ii)$$

Multiplying (i) and (ii), we get

$$\frac{h}{9} \times \frac{h}{4} = \tan \theta \times \cot \theta = 1$$

$$(\because \tan \theta \times \cot \theta = 1)$$

$$\Rightarrow \frac{h^2}{36} = 1 \Rightarrow h^2 = 36$$

$$\Rightarrow h = \pm 6 \text{ m}$$

$$\therefore h = 6 \text{ m } (\because \text{Height is positive only})$$

Thus, the height of the tower is 6 m.

Note : (**) marked question are deleted from NCERT.